# Comparing fractions with the same denominator

When comparing parts of the unit that are the same size, the fraction with the largest numerator is the greater fraction.

Ex) 
$$\frac{3}{10}$$
 <  $\frac{5}{10}$  I know this because 3 < 5.

Ex) Katherine ate  $\frac{2}{6}$  of a pizza. Patrick ate  $\frac{4}{6}$  of a pizza. Who ate more?

$$\frac{2}{6}$$
  $<$   $\frac{4}{6}$ 

Patrick ate more pizza. I know this because 2 < 4.

# Comparing fractions with the same numerator

When comparing fractions with different sized parts, the fraction with the smallest denominator is the greater fraction.

Ex) 
$$\frac{2}{8} > \frac{2}{10}$$
 I know this because  $\frac{1}{8} > \frac{1}{10}$ 

Ex) Julianne ate 3 slices of a pizza cut into 6 pieces. Sarah ate 3 slices of a pizza cut into 8 pieces. Who ate more?

$$\frac{3}{6} > \frac{3}{8}$$
 Julianne ate more pizza. I know this because  $\frac{1}{6} > \frac{1}{8}$ 

### Transitive Strategy: Using $\frac{1}{2}$ as a benchmark

When comparing fractions and the denominators are even, compare the fractions to the unit fraction  $\frac{1}{2}$ .

Ex) 
$$\frac{3}{8} < \frac{4}{6}$$

Ex)  $\frac{3}{6}$  I know this because  $\frac{1}{2} = \frac{4}{8}$  and  $\frac{1}{2} = \frac{3}{6}$ .

So if 
$$\frac{3}{8} < \frac{4}{8}$$
 and  $\frac{4}{6} > \frac{3}{6}$  then  $\frac{3}{8} < \frac{4}{6}$ 

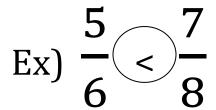
Ex) Katie ate  $\frac{4}{10}$  of a pizza and Mal ate  $\frac{3}{4}$  of a pizza. Who ate more?

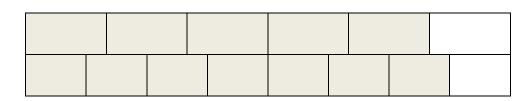
$$\frac{4}{10} < \frac{3}{4}$$

I know this because  $\frac{1}{2} = \frac{5}{10}$  and  $\frac{1}{2} = \frac{2}{4}$ . So if  $\frac{5}{10} > \frac{4}{10}$  and

$$\frac{2}{4}$$
 then  $\frac{4}{10}$   $\frac{3}{4}$ . Therefore, Mal ate more pizza.

#### Residual Strategy: Fill the whole

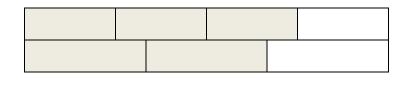




I know this because the missing  $\frac{1}{6}$  part is smaller than the missing  $\frac{1}{8}$  part. So if  $\frac{7}{8}$  is closer to 1 whole, then  $\frac{5}{6} < \frac{7}{8}$ .

Ex) Kelly ate  $\frac{3}{4}$  of a pizza and Greg ate  $\frac{2}{3}$  of a pizza. Who ate more?

$$\frac{3}{4} > \frac{2}{3}$$



I know this because the missing  $\frac{1}{4}$  part is smaller than the missing  $\frac{1}{3}$  part. So if  $\frac{3}{4}$  is closer to 1 whole, then  $\frac{3}{4} > \frac{2}{3}$ .

Therefore, Kelly ate more pizza than Greg.

### Comparing fractions with related denominators

Change one denominator, and then compare the new fractions.

Ex) 
$$\frac{6}{5} < \frac{13}{10}$$
 I know  $\frac{6}{5} = \frac{12}{10}$ . So if  $\frac{12}{10} < \frac{13}{10}$ , then  $\frac{6}{5} < \frac{13}{10}$ .

Ex) Kyle ate  $\frac{4}{6}$  of a pizza. Jess ate  $\frac{7}{12}$  of a pizza. Who ate more?

$$\frac{4}{6}$$
 >  $\frac{7}{12}$  I know  $\frac{4}{6} = \frac{8}{12}$ . So if  $\frac{8}{12}$  >  $\frac{7}{12}$ , then  $\frac{4}{6}$  >  $\frac{7}{12}$ .

Therefore, Kyle ate more pizza than Jess.

### Comparing non related fractions

Find the Least Common Multiple and change both denominators, then compare the new fractions.

Ex) 
$$\frac{4}{7} < \frac{2}{3}$$

Least Common Multiple:

7 14 21 28

3 6 9 12 15 18 21 24

I know 
$$\frac{4}{7} = \frac{12}{21}$$
 and  $\frac{2}{3} = \frac{14}{21}$ .

So if 
$$\frac{12}{21} < \frac{14}{21}$$
, then  $\frac{4}{7} < \frac{2}{3}$ .

Ex) Mary ate  $\frac{5}{9}$  of a pizza. Alex ate  $\frac{3}{4}$  of a pizza. Who ate more?

$$\frac{5}{9} < \frac{3}{4}$$

I know 
$$\frac{5}{9} = \frac{20}{36}$$
 and  $\frac{3}{4} = \frac{27}{36}$ . So if  $\frac{20}{36} < \frac{27}{36}$ 

then  $\frac{5}{6} < \frac{3}{4}$ . Therefore, Alex at more than Mary.

Least Common Multiple:

9 18 27 36 45 54 63

12 16 20 24 28 32 36